



# **Université Toulouse 1 Capitole Ecole d'économie de Toulouse**

Année universitaire 2016-2017

**Session 1** 

Semestre 2

Master 1 Economics, Econometrics Statistics

Epreuve: Environmental & Resource Economics

Date de l'épreuve : 29 mars 2017

Durée de l'épreuve : 1h30

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Calculator but no devices with storage capacity like smartphones, laptops, etc.

Nombre de pages (y compris page de garde): 3

# **Environmental & Resource Economics**

# **Toulouse School of Economics, Master 1**

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# Exam, Spring 2017, Session 1

### Question 1 (5p)

You are asked to use the monetary value for "clean air" from "Area A" (where a value has been estimated) in "Area B" (where no value has been estimated), i.e. you are asked to conduct a benefit transfer (BT). Since you have information about income differences between A and B you will use BT transfer with an income adjustment. You have access to the following info:

- The willingness to pay (WTP) for clean air in area A has been estimated to be 120 €
- The empirical evidence shows that the income elasticity of WTP is 0.5
- The mean income level in area A is 10 000 €
- The mean income level in area B is 40 000 €

Q1.a.: Estimate the BT value for Area B (i.e. the WTP for area B based on the BT approach).

Q1.b: Assume now that a study is conducted in area B that finds that the true WTP in B is 200 €. What is the transfer effort (TE) in percentage (as defined in the course) from using the BT value that you estimated above?

#### Question 2 (5p)

Estimate the effect on two firm's emissions levels (x) from the introduction of a Pigouvian tax (p). You have information about the two firms' (A and B) total cost functions:

$$TC_A = 1000 + 150x + 1.5x^2 + px$$

$$TC_B = 1200 + 120x + x^2 + px$$

Q2.a: Assume p=0, estimate the firms optimal emission level (x).

Q2.b: Assume p=30, estimate the firms optimal emission level (x) and calculate the change in emission from p=30 for both firms.

#### Question 3 (5p)

Consider the nonrenewable resource where remaining reserves evolve according to the iterative equation  $R_{t+1}=R_t-q_t$ , with  $R_0>0$  given. The net revenue from extraction  $q_t$  is given by  $\pi_t=pq_t-\left(\frac{c}{2}\right)q_t^2$ . The standard discount factor  $\rho=\frac{1}{(1+\delta)}$ . The current value Lagrangian to this problem can be

written as: 
$$\mathcal{L} = \sum_{t}^{\infty} \rho^t \left\{ pq_t - \left(\frac{c}{2}\right)q_t^2 + \rho\lambda_{t+1}(R_{t+1} - R_t - q_t) \right\}$$
, where  $\rho\lambda_{t+1}$  is the Lagrange multiplier.

Q3.a: Derive the necessary first order conditions and show that  $\lambda_t = \lambda_0 (1 + \delta)^t$ .

Q3.b: Suppose that the remaining reserves will be completely exhausted at a given future dates t=T, implying  $R_T=q_T=0$  and there is no further exploration. Evaluating the first order conditions at t=T implies  $p=\rho\lambda_{T+1}=\lambda_T=\lambda_0(1+\delta)^T$  and  $\lambda_0=p(1+\delta)^{-T}$ . What is the optimal extraction path? How would you proceed to obtain the optimal date of exhaustion T\*? (you don't need to derive T\*, however you should show the main assumptions that allow you to solve for the optimal date of exhaustion)

Q3.c: Describe the concept of resource scarcity (in maximum 3 sentences).

#### Question 4 (5p)

Consider an economy with a representation agent having a constant relative risk aversion  $\gamma=2$ , and a constant rate of impatience  $\delta=1\%$ . Let  $c_i$  denote consumption at date t. Suppose that  $c_i$  follows a geometric Brownian motion with trend  $\mu=2\%$  and a high volatility of  $\sigma=10\%$ .

- 1. Compute the term structures of risk-free discount rates and risk premia.
- 2. Evaluate the NPV of the following two projects: All projects have an initial cost  $\varepsilon$  today.
  - Project A yields a single benefit of  $1.1\varepsilon$  in 10 years.
  - Project B yields a single benefit of  $30\varepsilon$  in 100 years.
- 3. Project C yields a sure cost of  $\varepsilon$  today and an uncertain benefit of  $\varepsilon k \left(c_{100} / c_0\right)^2$  in 100 years, where k is a positive constant.
  - Which risk-adjusted discount rate should we use for this project?
  - What is the expected benefit of this project?
  - Estimate the NPV of this project. What is the minimum value of k that makes it desirable?